

1) The electronic polarizability of the Ar atom has a value of $1.7 \times 10^{-40} \text{ F m}^2$. What is the static dielectric constant of the solid Ar if its density is 1.8 g cm^{-3} and its atomic mass is 39.95 g mol^{-1} ? (Avogadro's number = $6.02 \times 10^{23} \text{ mol}^{-1}$).

2) Consider a CsCl crystal which has CsCl unit cell crystal structure (one $\text{Cs}^+ \text{Cl}^-$ pair per unit cell) with a lattice parameter (a) of 0.412 nm . The electronic polarizability of Cs^+ and Cl^- ions are $3.35 \times 10^{-40} \text{ F m}^2$ and $3.4 \times 10^{-40} \text{ F m}^2$ respectively, and the mean ionic polarizability per ion pair is $6 \times 10^{-40} \text{ F m}^2$. What is the dielectric constant? (Given that $N = 1/a^3$).

3) In a certain atom, the positive charge in the nucleus has a value of $q = 3.2 \times 10^{-19} \text{ C}$, the radius of the atom $R = 6 \times 10^{-9} \text{ cm}$, $E = 20 \text{ KV/cm}$ and $N = 3 \times 10^{19} \text{ cm}^{-3}$. Find the equilibrium distance d_E , the dielectric susceptibility and dielectric constant resulting from electronic polarization.

4) An atom with a radius of 5×10^{-8} cm has a positive charge in the nucleus with a magnitude of 4×10^{-18} C. If the atom is subjected to an electrical field of 15KV/cm, calculate the equilibrium distance "d" according to the electronic polarization assuming a number of molecules per unit volume of 25×10^{20} . Calculate also the electric dipole moment, the polarization, the dielectric susceptibility and the dielectric constant after equilibrium.

5) Find the polarizability of a certain ion in Fm^2 assuming that the number of molecules per unit volume is $22 \times 10^{18} \text{ cm}^{-3}$. The dielectric constant of the ion is 4.

$$N = 22 \times 10^{18}$$

$$\epsilon_r = 4$$

$$\frac{\epsilon_r - 1}{\epsilon_r + 2} = \frac{N \alpha}{3 \epsilon_0}$$

$$\alpha = 6.634 \times 10^{-37} \text{ Fm}^2$$

$$\epsilon_r = 1 + \frac{N \alpha_0}{\epsilon_0 (1 + \omega^2 \tau^2)}$$

1) For the orientation polarization with sinusoidal applied field, find the expressions for ϵ'_r and ϵ''_r .

2) With the help of equations 1-6, 1-8 and 2-4, derive equations to describe the variation of the dielectric constant with frequency. Assume that $\alpha_0 = 6 \times 10^{-36} \text{ F m}^2$ and $N = 25 \times 10^{22} \text{ m}^{-3}$. Plot this variation when the frequency varies in the range from $0.001/\tau$ to $1000/\tau$.

3) Obtain the dielectric loss per unit capacitance in a capacitor in terms of the loss tangent. Obtain the phase difference between the current through the capacitor and that through R_p . What is the significance of δ ?

4) Calculate the power dissipated per unit volume of cross-linked polyethylene, XLPE (typical power cable insulator) at 60 Hz at a field of 100 kV cm^{-1} if ϵ'_r and $\tan \delta$ of XLPE are 2.3 and 3×10^{-4} respectively.

$$P = \omega \cdot \epsilon'' \cdot E^2$$